# Tree structured CRF models for interactive image labeling

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### Outline

1. Introduction

2. Structured image annotation models

3. Label Elicitation

4. Experimental Evaluation

5. Attribute-based image classification













Sky, Tree, Building, Sea, Plant, Ground, Rock, Person, Windows, Sand, Water.







- Sky, Tree, Building, Sea, Plant, Ground, Rock, Person, Windows, Sand, Water.
- Ask the user: Building (false), Rock (true), Sea (true), ...







- Sky, Tree, Building, Sea, Plant, Ground, Rock, Person, Windows, Sand, Water.
- Ask the user: Building (false), Rock (true), Sea (true), ...
- Update the ranked list of keywords based on this information





### Introduction - 1

- Image labeling problem, a.k.a. classification, annotation, attribute prediction,...
- Used for e.g.: keyword based retrieval, indexing, clustering, ...
- State of the art: train binary SVMs per label using fancy features (SIFT, Bow, Fisher Kernels, spatial pyramids, ...)





### Introduction - 1

- Image labeling problem, a.k.a. classification, annotation, attribute prediction,...
- Used for e.g.: keyword based retrieval, indexing , clustering, ...
- State of the art: train binary SVMs per label using fancy features (SIFT, Bow, Fisher Kernels, spatial pyramids, ...)
- Problem 1: it ignores structure in output, correlation between labels (*e.g.* car & indoor).
- **Problem 2**: how to incorporate user input





### Introduction - 2

- How to obtain a (tractable) structure?
- How to learn the parameters of this structure?
- How to select labels to ask the user?
- How does it perform?





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- Learn weights between nodes to encode co-occurrence.
- Exact inference in tree structure is tractable (using BP).
- Inference is used for learning, label prediction and label elicitation.





### Tree structured model on image labels

- Each node presents a label in the tree.
- Vector of (binary) labels:  $\mathbf{y} = \{y_1, \dots, y_L\}$ .
- Edges (L-1) are (somehow) given:  $\mathcal{E} = \{e_1, \ldots, e_{L-1}\}$ .

$$E(\boldsymbol{y}, \boldsymbol{x}) = \sum_{i=1}^{L} \psi_i(\boldsymbol{y}_i, \boldsymbol{x}) + \sum_{(i,j) \in \mathcal{E}} \psi_{ij}(\boldsymbol{y}_i, \boldsymbol{y}_j), \quad (1)$$

$$p(\boldsymbol{y}|\boldsymbol{x}) = \frac{1}{Z(\boldsymbol{x})} \exp -E(\boldsymbol{y}, \boldsymbol{x}), \qquad (2)$$

$$Z(\boldsymbol{x}) = \sum_{\boldsymbol{y} \in \{0,1\}^L} \exp - E(\boldsymbol{y}, \boldsymbol{x})$$
(3)





### **Unary Potentials**

$$E(\boldsymbol{y}, \boldsymbol{x}) = \underbrace{\sum_{i=1}^{L} \psi_i(\boldsymbol{y}_i, \boldsymbol{x})}_{\text{Unary Potentials}} + \sum_{\substack{(i,j) \in \mathcal{E} \\ \psi_{ij}(\boldsymbol{y}_i, \boldsymbol{y}_j)}} \psi_{ij}(\boldsymbol{y}_i, \boldsymbol{y}_j)$$



■  $y_i$  is a label Rock, Sea, City, People,... ■  $\psi_i(y_i = l, \mathbf{x}) = [\phi_i(\mathbf{x}), 1]^\top \mathbf{w}_i^l$ 

•  $\phi_i(\mathbf{x})$ : Pre-trained SVM score for label i





### **Pairwise Potentials**

$$E(\boldsymbol{y}, \boldsymbol{x}) = \sum_{i=1}^{L} \psi_i(\boldsymbol{y}_i, \boldsymbol{x}) + \underbrace{\sum_{(i,j)\in\mathcal{E}} \psi_{ij}(\boldsymbol{y}_i, \boldsymbol{y}_j)}_{\text{Pairwise Potentials}}$$



y<sub>i</sub> = Sand, and y<sub>i</sub> = City
 Independent of image input

$$\Psi_{ij}(\mathbf{y}_i = \mathbf{s}, \mathbf{y}_j = t) = \mathbf{v}_{ij}^{st}$$





# Defining the Tree

Optimal tree structure for conditional models is intractableFor generative models use the Chow-Liu algorithm



- Fully connected graph
- Edge weight = Mutual Information
- Maximum Spanning Tree





### Learning

Learning *w* and *v* in unary and pairwise potentials
Using Log-likelihood (concave):

$$\mathcal{L} = \sum_{n=1}^{N} \mathcal{L}_n = \sum_{n=1}^{N} \ln p(\boldsymbol{y}_n | \boldsymbol{x}_n).$$

Gradients:

$$\frac{\partial \mathcal{L}_n}{\partial \boldsymbol{w}_i^l} = \left( p(\boldsymbol{y}_i = l | \boldsymbol{x}_n) - \llbracket \boldsymbol{y}_{in} = l \rrbracket \right) \phi_i(\boldsymbol{x}_n), \quad (4)$$
$$\frac{\partial \mathcal{L}_n}{\partial \boldsymbol{v}_{ij}^{st}} = p(\boldsymbol{y}_i = \boldsymbol{s}, \boldsymbol{y}_j = t | \boldsymbol{x}_n) - \llbracket \boldsymbol{y}_{in} = \boldsymbol{s}, \boldsymbol{y}_{jn} = t \rrbracket, \quad (5)$$





### Trees over groups of labels







### Trees over groups of labels



- To allow more dependencies between labels
- A node is a group of fully connected labels.
- Every state modeled explicitly, a node has  $2^k$  states.
- To define a tree-structure
  - Agglomerative clustering of labels,
  - Chow-Liu algorithm on these clusters.





# **Compund Node**

| arease and | - |                       |                    | -         |
|------------|---|-----------------------|--------------------|-----------|
|            |   | and the second second | CHARDEN CONTRACTOR | PIDINE IN |
|            |   |                       |                    | _         |

| State                    | Marginal | Landscape/Nature | Sky   | Clouds |
|--------------------------|----------|------------------|-------|--------|
| 1                        | 3.4 %    | 0                | 0     | 0      |
| 2                        | 0.0 %    | 0                | 0     | 1      |
| 3                        | 9.8 %    | 0                | 1     | 0      |
| 4                        | 59.9 %   | 0                | 1     | 1      |
| 5                        | 0.4 %    | 1                | 0     | 0      |
| 6                        | 0.0 %    | 1                | 0     | 1      |
| 7                        | 2.6 %    | 1                | 1     | 0      |
| 8                        | 23.9 %   | 1                | 1     | 1      |
| Marginal on label = true |          | 26.9%            | 96.2% | 83.8%  |

- BP gives us node marginals,
- read-off label marginals  $p(y_i | \mathbf{x})$ .
- message passing: O(2<sup>2k</sup>)





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#### SUN 09 - 5 labels



BeforeQuestions01 Sky02 Tree03 Building04 Sea05 Rocks06 Plant07 Ground08 Rock09 Person10 Window





#### SUN 09 - 5 labels



Questions Before 01 Sky 02 Tree 03 Building 04 Sea 05 Rocks 06 Plant 07 Ground 08 Rock 09 Person 10 Window

Building





#### SUN 09 - 5 labels



Questions Before 01 Sky 02 Tree 03 Building 04 Sea 05 Rocks 06 Plant 07 Ground 08 Rock 09 Person 10 Window

Building Tree







| Before              | Questions |
|---------------------|-----------|
| 01 Sky              |           |
| 02 Tree             |           |
| 03 Building         |           |
| 04 <mark>Sea</mark> | Building  |
| 05 Rocks            | Tree      |
| 06 Plant            | Sea       |
| 07 Ground           |           |
| 08 Rock             |           |
| 09 Person           |           |
| 10 Window           |           |







| Before              | Questions |
|---------------------|-----------|
| 01 <mark>Sky</mark> |           |
| 02 Tree             |           |
| 03 Building         |           |
| 04 <mark>Sea</mark> | Building  |
| 05 Rocks            | Tree      |
| 06 Plant            | Sea       |
| 07 Ground           | Rocks     |
| 08 Rock             |           |
| 09 Person           |           |
| 10 Window           |           |







| Before              | Questions |
|---------------------|-----------|
| 01 <mark>Sky</mark> |           |
| 02 Tree             |           |
| 03 Building         |           |
| 04 <mark>Sea</mark> | Building  |
| 05 Rocks            | Tree      |
| 06 Plant            | Sea       |
| 07 Ground           | Rocks     |
| 08 Rock             | Rock      |
| 09 Person           |           |
| 10 Window           |           |







| Before              |
|---------------------|
| 01 <mark>Sky</mark> |
| 02 Tree             |
| 03 Building         |
| 04 <mark>Sea</mark> |
| 05 Rocks            |
| 06 Plant            |
| 07 Ground           |
| 08 Rock             |
| 09 Person           |
| 10 Window           |

| Questions | After               |
|-----------|---------------------|
|           | 01 Rock             |
|           | 02 Rocks            |
|           | 03 <mark>Sea</mark> |
| Building  | 04 <mark>Sky</mark> |
| Tree      | 05 Sand             |
| Sea       | 06 Ground           |
| Rocks     | 07 Plant            |
| Rock      | 08 Person           |
|           | 09 Window           |
|           | 10 Water            |





- interactive setting: Ask the user at *test* time to set some of many labels for a single example.
- **active learning:** Ask the user at *train* time for class label of some of many examples.





Select a label *i* such that expected uncertainty in remaining labels is minimized:

$$H(\mathbf{y}_{\setminus i}|y_i,\mathbf{x}) = \sum_{l} p(y_i = l|\mathbf{x}) H(\mathbf{y}_{\setminus i}|y_i = l,\mathbf{x}).$$

Entropy Identity:

$$H(\boldsymbol{y}|\boldsymbol{x}) = H(y_i|\boldsymbol{x}) + H(\boldsymbol{y}_{\setminus i}|y_i,\boldsymbol{x})$$

Equals to select label *i* with highest entropy  $H(y_i | \mathbf{x})$ .





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### Databases

### Table: Basic statistics of the three data sets.

|                      |       | ImageCLEF  | SUN'09 | Animals w.A. |
|----------------------|-------|------------|--------|--------------|
| # Train images       |       | 6400       | 4367   | 24295        |
| # Test images        |       | 1600       | 4317   | 6180         |
| # Labels             |       | 93         | 107    | 85           |
| Train img/label      |       | 833        | 219    | 8812         |
| Train label/img      |       | 12.1       | 5.34   | 30.8         |
| Nr of parameters for | k = 1 | $\pm$ 740  | 852    | 676          |
| trees with           | k = 2 | $\pm 1284$ | 1480   | 1172         |
| group size           | k = 3 | $\pm 2912$ | 3340   | 2644         |
|                      | k = 4 | ±7508      | 8640   | 6836         |

Performance evaluated using:

- MAP: retrieval performance per label,
- iMAP: annotation performance per image.





### **Results 1**







### **Results 1**







### Results 2



Interactive image annotation performance as a function of the amount of user input, ImageCLEF dataset





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### Attribute-based image classification

#### otter

black: yes white: no brown: stripes: no water: ves eats fish: ves

#### polar bear

black. no white: yes brown: no stripes: no water: ves eats fish: yes

#### zebra

black: ves white: yes brown: no stripes: ves water: no eats fish: no





- images x,
- ▶ class labels  $y_1, \ldots, y_K \in \mathcal{Y}$  (at training time)
- class labels  $z_1, \ldots, z_L \in \mathcal{Z}$  (at test time)
- ▶ attributes  $a_1, \ldots, a_M \in \{0, 1\}^M$  (encode description)





## Attribute-based image classification - 2

Predict attributes with our tree-structured models.





## Attribute-based image classification - 2

- Predict attributes with our tree-structured models.
- Deterministic mapping between attributes and classes.

$$p(z=c|\boldsymbol{x}) = \frac{p(\boldsymbol{y}_c|\boldsymbol{x})}{\sum_{c'=1}^{C} p(\boldsymbol{y}_{c'}|\boldsymbol{x})} = \frac{\exp -E(\boldsymbol{y}_c, \boldsymbol{x})}{\sum_{c'=1}^{C} \exp -E(\boldsymbol{y}_{c'}, \boldsymbol{x})}.$$
 (6)

Note: does not require belief-propagation, it suffices to evaluate  $E(\mathbf{y}_c, \mathbf{x})$  for the *C* attribute configurations.





# **Correction Term**

Observation: some classes are over-predicted:

$$p(z = c | \boldsymbol{x}) \propto \exp\left(-E(\boldsymbol{y}_c, \boldsymbol{x}) - u_c\right),$$
 (7)







### Label Elicitation for classification

Label Elicitation on Attribute Level





### Label Elicitation for classification

- Label Elicitation on Attribute Level
- Goal to minimize uncertainty on class label
- Any informative question rules out at least 1 class.





### Label Elicitation for classification

- Label Elicitation on Attribute Level
- Goal to minimize uncertainty on class label
- Any informative question rules out at least 1 class.
- Results (again) in attribute *i* with highest entropy H(y<sub>i</sub>|x).
  But p(y<sub>i</sub>|x) is defined differently:

$$p(y_i = 1 | \boldsymbol{x}) = \sum_{c} p(z = c | \boldsymbol{x}) y_{ic}, \quad (8)$$





### **Results Classification**

|       | Init | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8     |
|-------|------|------|------|------|------|------|------|------|-------|
| Indep | 36.5 | 53.1 | 68.5 | 77.8 | 85.1 | 90.6 | 94.5 | 97.7 | 99.4  |
| Mixt  | 38.7 | 55.3 | 72.3 | 84.8 | 92.4 | 96.9 | 99.0 | 99.8 | 100.0 |

- classification accuracy of the independent and mixture of trees models.
- Initial results, and after user input for one up to eight selected attributes.





## Conclusions

### Tree-structured CRF models for interactive

- Image annotation, and
- Attribute-based classification
- Improves moderately over independent models
- Real power in interactive setting: (i) propagate user input,
   (ii) ask more informative questions





# Tree structured CRF models for interactive image labeling

Questions?!?



