

# Sparse Coding and Dictionary Learning for Image Analysis

[http://www.di.ens.fr/~mairal/tutorial\\_iccv09/](http://www.di.ens.fr/~mairal/tutorial_iccv09/)



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# A hierarchy of Problems

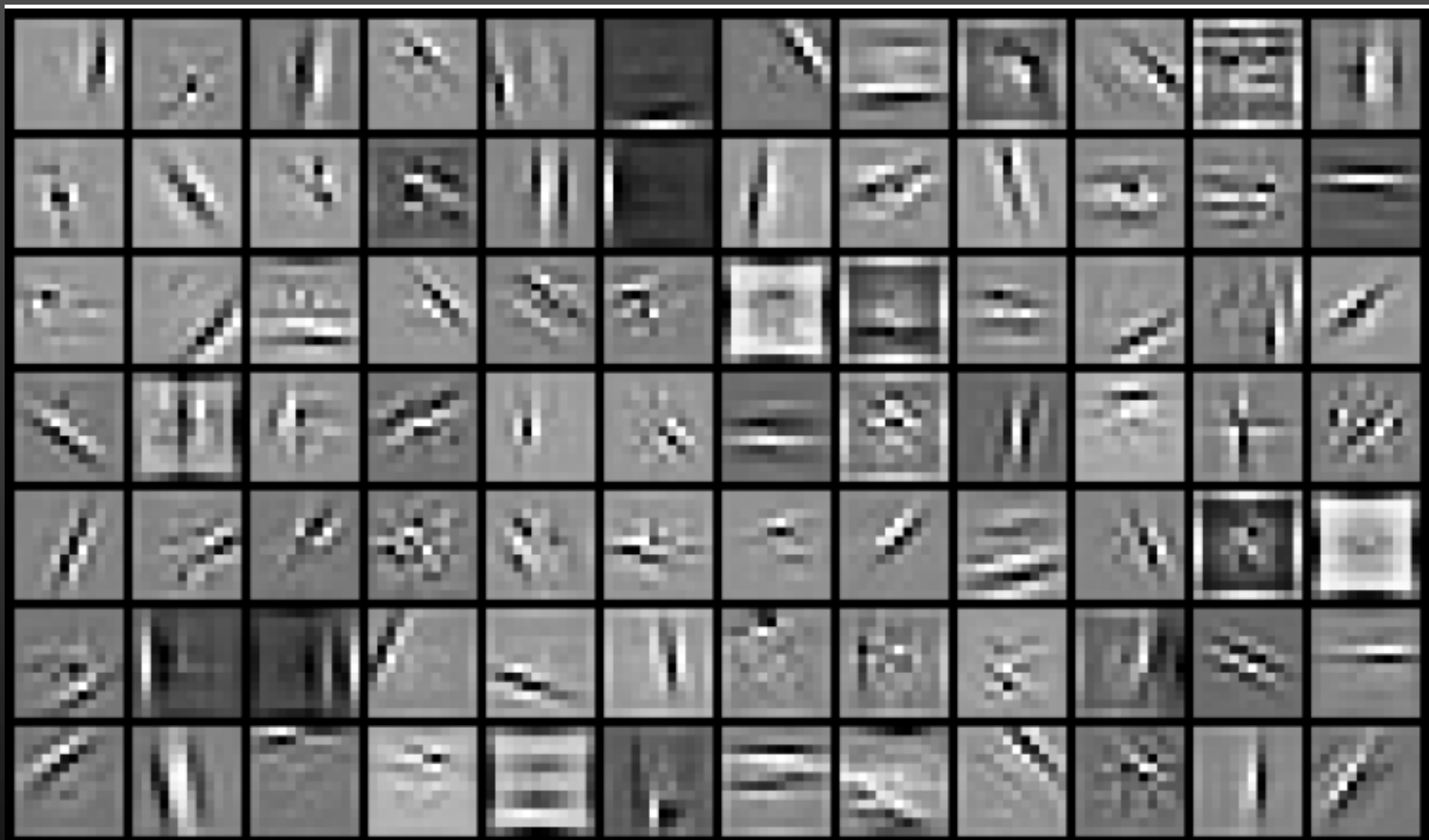
$$\min_{\alpha} \|x - D\alpha\|_2^2 + \lambda \|\alpha\|_0$$

$$\min_{\alpha} \|x - D\alpha\|_2^2 + \lambda \psi(\alpha)$$

$$\min_{D \in \mathcal{C}, \alpha_1, \dots, \alpha_n} \sum_{1 \leq i \leq n} [1/2 \|x_i - D\alpha_i\|_2^2 + \lambda \psi(\alpha_i)]$$

$$\min_{D \in \mathcal{C}, \alpha_1, \dots, \alpha_n} \sum_{1 \leq i \leq n} [f(x_i, D, \alpha_i) + \lambda \psi(\alpha_i)]$$

$$\min_{D \in \mathcal{C}, \alpha_1, \dots, \alpha_n} \sum_{1 \leq i \leq n} [f(x_i, D, \alpha_i) + \lambda \sum_{1 \leq j \leq p} \psi(d_j)]$$



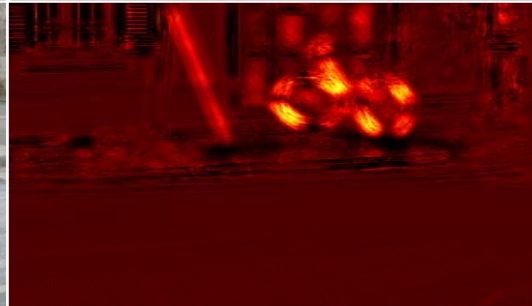
# Outline

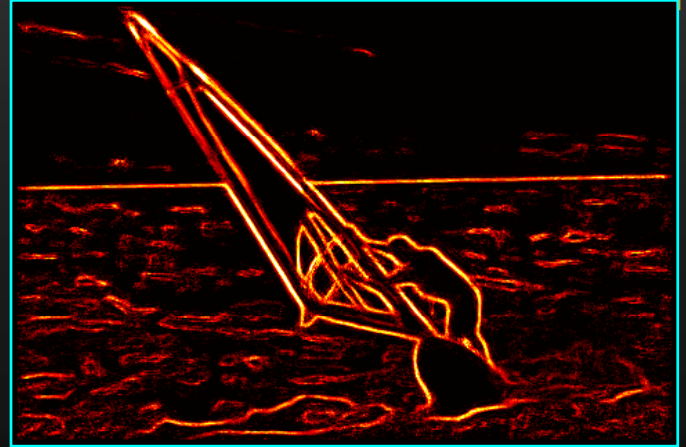
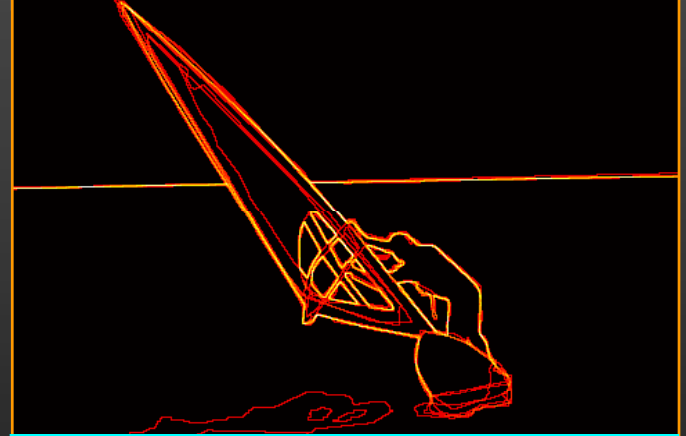
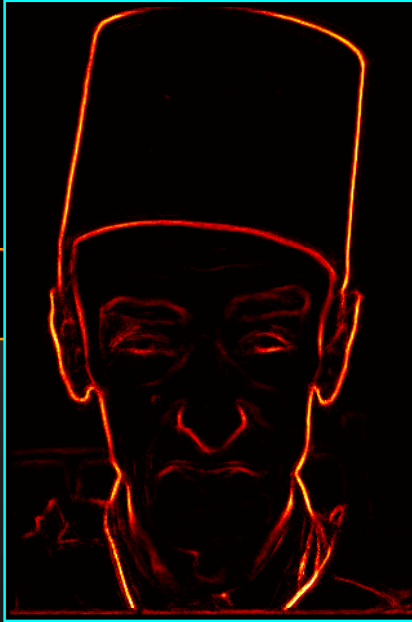
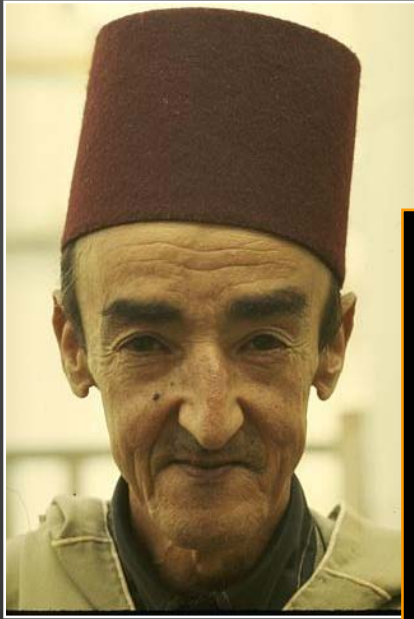
## Introduction

1. Optimization for Sparse Coding
2. Dictionary Learning for Reconstruction
3. Learning for the Task
4. New Sparse Models

Open Questions and Discussion

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*SPArse Modeling Software*  
*(SPAMS) available!*

<http://www.di.ens.fr/willow/SPAMS/>